

# Competitive blockage of the sodium channel by intracellular magnesium ions in central mammalian neurones

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**Abstract.** The aim of this study was to determine from macroscopic current analysis how intracellular magnesium ions,  $Mg_i^{2+}$ , interfere with sodium channels of mammalian neurones. It is reported here that permeation across the sodium channel is voltage- and concentration-dependently reduced by  $Mg_i^{2+}$ . This results in a general reduction of sodium membrane conductance and an outward sodium peak current at large positive potentials. 30 mM  $Mg_i^{2+}$  leads to a negative shift of voltage dependence of sodium channel gating parameters, probably due to the surface potential change of the membrane. This shift alone is, however, insufficient to explain the reduction of outward sodium currents. The blockage by  $Mg_i^{2+}$  is decreased upon increasing intracellular or extracellular  $Na^+$  concentration, which suggests that  $Mg_i^{2+}$  interferes with sodium permeation by competitively occupying sodium channels. Using a kinetic model to describe the sodium permeation, the dissociation constant (at zero membrane potential) of  $Mg_i^{2+}$  for the sodium channel has been calculated to be  $8.65 \pm 1.51$  mM, with its binding site located at  $0.26 \pm 0.05$  electrical distance from the inner membrane. This dissociation constant is smaller than that of  $Na_i^+$ , which is  $83.76 \pm 7.60$  mM with its binding site located at  $0.75 \pm 0.23$ . The low dissociation constant of  $Mg_i^{2+}$  reflects its high affinity for the sodium channel.

**Key words:** Sodium channel – Patch clamp – Cerebellar granule cells – Intracellular magnesium

## Introduction

Intracellular  $Mg^{2+}$  is involved in several cellular functions, by regulating various biochemical reactions (Strata and Benedetti 1988). The regulation of  $Mg_i^{2+}$  has been studied in different preparations (e.g. Altura and Altura 1985; Baker and Dipolo 1984). Intracellular  $Mg^{2+}$  is also known to interact with several ionic channels, such as the

*N*-methyl-D-aspartate-activated channel (Johnson and Ascher 1990), the ATP sensitive potassium channel (Horie et al. 1987), the muscarinic potassium channel (Horie and Irisawa 1987), the inward rectifier potassium channel (Matsuda 1988), and calcium channels (White and Hartzell 1988).

The reduction of outward currents through the sodium channel, expressed in *Xenopus* oocytes from rat brain cDNA, has also been described (Pusch et al. 1989; Pusch 1990). The cerebellar granule cell in culture has been recognized as an excellent model for studying electrophysiological (e.g. Hockberger et al. 1987; Cull-Candy et al. 1989; Sciancalepore et al. 1989; Lin and Moran 1990) and biochemical (e.g. Levi et al. 1984; Nicoletti et al. 1987) properties of neurones, owing to the fact that it maintains the morphological and functional properties of native neurones (Levi et al. 1984). We have, therefore, investigated in detail the effect of  $Mg_i^{2+}$  on macroscopic  $Na^+$  currents in cerebellar granule cells in order to study the possible kinetic mechanism of the  $Mg^{2+}$  blockage. From our results, we propose that  $Mg_i^{2+}$  blocks sodium channels by entering the sodium channel and binding to a site inside the pore with high affinity.

## Methods

### Cell preparation

Experiments were performed on cerebellar granule cells dissociated from eight days old Wistar rats, and prepared according to Levi and co-workers (1984). In order to diminish the problems of space-clamp produced by the neuritic processes growing, and of differences in the sodium channel expression during differentiation in vitro, cells were used only between 3 and 5 days in culture (DIC).

Bath solutions were (in millimolar):  $CaCl_2$  2,  $CoCl_2$  5, HEPES-NaOH (*N*-2-hydroxyethylpiperazine) 10 and  $NaCl$  40, 60 and 100 respectively. Pipette solutions, dialyzing the intracellular compartment, had different  $Na^+$  and  $Mg^{2+}$  concentration ( $[Na^+]_i$ ,  $[Mg^{2+}]_i$ ), as described

**Table 1.** Intracellular (pipette) solutions. Osmolarities of solutions were adjusted with *d*-glucose (see text)

Composition	15 Na <sup>+</sup> [mM]	20 Na <sup>+</sup> [mM]	30 Na <sup>+</sup> [mM]	30 Na <sup>+</sup> [mM]
NaCl	5	10	20	20
MgCl <sub>2</sub>	0, 0.5, 1, 3, 7	0, 0.5, 1, 2, 3, 5, 7	0, 0.5, 1, 3, 7	30
CsF	110	105	95	70
EGTA <sup>a</sup>	11	11	11	11
HEPES-NaOH	10	10	10	10

<sup>a</sup> EGTA: Ethyleneglycol-bis-β-amino-ethylether

in Table 1. Osmolarities of intracellular solutions were corrected to 295 mOsm and those of external solutions to 310 mOsm with *d*-glucose. In all solutions, pH was adjusted to 7.35. All experiments were performed at room temperature (17 to 21 °C).

### Voltage clamp experiments

Ionic currents were measured in the whole-cell configuration of the patch-clamp technique (Hamill et al. 1981), using a standard patch-clamp amplifier (EPC-7, List Medical Electronics). Patch pipettes were pulled from borosilicate glass pipettes (Hilgenberg) and had resistances in the range of 2.5 to 4 MΩ after fire polishing, and determined with our intracellular/extracellular working solutions. In all experiments, potassium currents were negligible because of intracellular substitution of K<sup>+</sup> with Cs<sup>+</sup>. Calcium currents were also insignificant under our experimental conditions owing to the presence of 5 mM Co<sup>2+</sup>, known to be very potent blocker of calcium channels (Brown et al. 1981; Carbone and Lux 1984). Holding potential was maintained at -90 mV. In all cases, the major part of the capacitive component of the membrane current in response to a voltage-step stimulation was compensated analogically. The full correction of capacitance and leak responses was made digitally on-line (see below).

### Data acquisition

Stimulation and data acquisition were controlled by a microcomputer (Atari 1040ST), equipped with a 12 bit A/D-D/A converter (M2-Lab, Instrutech). Before digital acquisition at 50 kHz, currents were low-pass filtered by a 4-pole Bessel filter (Ithaco, 4302), at a cut-off frequency of 5 kHz or 10 kHz.

Standard pulse protocols were used to study macroscopic properties of sodium currents. The voltage dependence of sodium current activation and kinetics of activation and inactivation were examined using a series of voltage pulses to various depolarizing levels between -40 and 130 mV, preceded by a -100 mV prepulse lasting 5 ms. Double-pulse stimulations composed of a fixed test pulse preceded by a 40 ms conditional test pulse to various voltage levels, from -80 mV to -5 mV, allowed

us to characterize the voltage dependence of steady-state sodium channel inactivation. All stimulations for sodium current measurements were followed by a similar pulse protocol in which pulse amplitudes were reduced to 1/4 and the holding potential was brought to -110 mV (P/4 procedure, Bezanilla and Armstrong 1977). The P/4 responses were used to subtract linear membrane responses.

### Data analysis

Voltage-dependent properties of sodium currents were analysed in terms of the Hodgkin and Huxley model (Hodgkin and Huxley 1952). The peak sodium current  $I_p$  was estimated by fitting the experimental record in a short interval around the peak with a third order polynomial. Means of peak currents were obtained from between 4 and 26 patches at each ionic concentration. All the fitting procedures are based on the standard least-square procedure (Press et al. 1989).

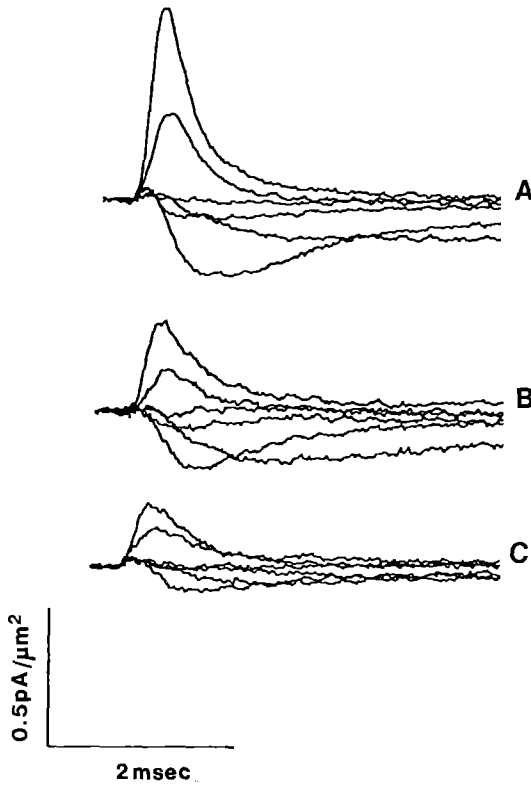
## Results

### *Mg<sup>2+</sup> blocking effect on the sodium channel is concentration and voltage dependent*

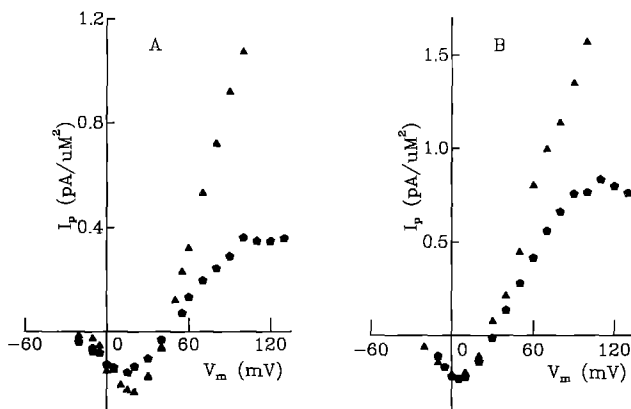
Macroscopic sodium currents were recorded in the whole-cell configuration of the patch-clamp technique, from -40 to 130 mV with different [Mg<sup>2+</sup>]<sub>i</sub>. In order to compare results obtained from different cells, currents were scaled by membrane area, calculated from the compensation of the capacity transient of each cell (using the empirical relation: 1 pF/100 μm<sup>2</sup>). The scaled maximum inward peak current measured from 3–5 DIC cells is 0.26 ± 0.08 pA/μm<sup>2</sup> (mean ± SD, *n* = 21 and Na<sub>i</sub><sup>+</sup>/Na<sub>o</sub><sup>+</sup> = 15/110). The membrane capacity is 2.2 ± 0.3 pF (mean ± SD, *n* = 63). Figure 1 shows families of sodium currents obtained with different [Mg<sup>2+</sup>]<sub>i</sub>. It illustrates that the blocking effect of Mg<sub>i</sub><sup>2+</sup> on sodium current increases upon increasing [Mg<sup>2+</sup>]<sub>i</sub>.

Relations of peak current to test potential,  $I_p - V_m$ , obtained at [Na<sup>+</sup>]<sub>i</sub> = 15 mM, 0 mM and 7 mM Mg<sub>i</sub><sup>2+</sup> are shown in Fig. 2A. Sodium peak currents appear to be reduced at applied  $V_m > 0$  mV in the presence of Mg<sub>i</sub><sup>2+</sup>. However, this reduction of sodium current becomes striking when  $V_m$  is higher than the sodium equilibrium potential. The blocking effect of 7 mM [Mg<sup>2+</sup>]<sub>i</sub> is still clearly observed when the intracellular Na<sup>+</sup> concentration is raised to 30 mM, as is shown in Fig. 2B. Nevertheless, the reduction of  $I_p$  by Mg<sub>i</sub><sup>2+</sup>, especially on the inward currents, diminished upon increasing [Na<sup>+</sup>]<sub>i</sub>.

In order to evaluate the blocking effect of Mg<sub>i</sub><sup>2+</sup> under different experimental conditions, we normalized the peak current obtained in the presence of Mg<sub>i</sub><sup>2+</sup> by that in the absence of Mg<sub>i</sub><sup>2+</sup>. Normalized peak currents,  $I_n$ , obtained at 15 mM and 30 mM Na<sub>i</sub><sup>+</sup> are compared in Table 2. It is shown that the blocking effect of Mg<sub>i</sub><sup>2+</sup> increases when the intracellular Mg<sub>i</sub><sup>2+</sup> concentration is increased. However, the same [Mg<sup>2+</sup>]<sub>i</sub> leads a lower



**Fig. 1A–C.** Families of sodium currents obtained from three whole-cell patches. The holding potential was maintained at  $-90$  mV. Voltage pulses to various test potentials from  $-20$  to  $-80$  mV in  $20$  mV steps, were preceded by a  $5$  ms prepulse of  $-100$  mV. Each trace is the average of  $8$  records after the subtraction of linear leakage and capacitance currents. **A** was obtained with  $0$  mM  $[\text{Mg}^{2+}]_i$ , **B** with  $0.5$  mM  $[\text{Mg}^{2+}]_i$  and **C** with  $7$  mM  $[\text{Mg}^{2+}]_i$ . All currents have been corrected by membrane areas.  $[\text{Na}^+]_i = 15$  mM and  $[\text{Na}^+]_o = 110$  mM



**Fig. 2A, B.** Peak current ( $I_p$ )-membrane voltage ( $V_m$ ) relationships. Triangles represent  $I_p$  obtained at  $[\text{Mg}^{2+}]_i = 0$  mM and pentagons are values obtained at  $[\text{Mg}^{2+}]_i = 7$  mM. Results were obtained from  $4$  different cells. **A** Peak currents were obtained at  $[\text{Na}^+]_i = 15$  mM. Reversal potentials are  $43.7$  mV and  $43.4$  mV, in the presence of  $0$  and  $7$  mM  $\text{Mg}^{2+}$  respectively. **B** Peak currents were obtained at  $[\text{Na}^+]_i = 30$  mM. Reversal potentials are  $28.5$  mV and  $29.8$  mV in the presence of  $0$  and  $7$  mM  $\text{Mg}^{2+}$ . All peak currents have been corrected by membrane areas.  $[\text{Na}^+]_o = 110$  mM in both cases

**Table 2.** Normalized mean peak currents ( $I_n$ ) obtained at an applied potential of  $100$  mV, and different  $[\text{Na}^+]_i$  and  $[\text{Mg}^{2+}]_i$ . Values represent mean  $\pm$  SD.  $[\text{Na}^+]_o$  is fixed at  $110$  mM

$[\text{Mg}^{2+}]_i$	$I_n$ ( $[\text{Na}^+]_i = 15$ mM)	$I_n$ ( $[\text{Na}^+]_i = 30$ mM)
0.0	$1.00 \pm 0.08$ ( $n=20$ )	$1.00 \pm 0.07$ ( $n=26$ )
0.5	$0.67 \pm 0.07$ ( $n=9$ )	$0.84 \pm 0.08$ ( $n=4$ )
3.0	$0.51 \pm 0.09$ ( $n=9$ )	$0.64 \pm 0.04$ ( $n=3$ )
7.0	$0.35 \pm 0.07$ ( $n=6$ )	$0.47 \pm 0.04$ ( $n=6$ )

**Table 3.** Normalized mean peak currents ( $I_n$ ) obtained at an applied potential of  $100$  mV, and different  $[\text{Na}^+]_o$  and  $[\text{Mg}^{2+}]_i$ . Values represent mean  $\pm$  SD.  $[\text{Na}^+]_i$  is fixed at  $30$  mM

$[\text{Mg}^{2+}]_i$	$I_n$ ( $[\text{Na}^+]_o = 50$ mM)	$I_n$ ( $[\text{Na}^+]_o = 70$ mM)	$I_n$ ( $[\text{Na}^+]_o = 110$ mM)
0.0	$1.00 \pm 0.13$ ( $n=10$ )	$1.00 \pm 0.07$ ( $n=16$ )	$1.00 \pm 0.07$ ( $n=26$ )
1.0	$0.70 \pm 0.10$ ( $n=8$ )	$0.73 \pm 0.05$ ( $n=10$ )	$0.78 \pm 0.09$ ( $n=4$ )
3.0	$0.56 \pm 0.07$ ( $n=8$ )	$0.60 \pm 0.06$ ( $n=10$ )	$0.64 \pm 0.04$ ( $n=3$ )
7.0	$0.43 \pm 0.10$ ( $n=7$ )	$0.45 \pm 0.10$ ( $n=9$ )	$0.47 \pm 0.04$ ( $n=6$ )

**Table 4.** The time to peak (ms), evaluated at different applied membrane potentials. Values are mean  $\pm$  SD. ( $[\text{Na}^+]_i = 15$  mM,  $[\text{Na}^+]_o = 110$  mM)

$[\text{Mg}^{2+}]_i$	$10$ mV	$80$ mV	$100$ mV	N
0.0	$1.57 \pm 0.17$	$0.47 \pm 0.04$	$0.47 \pm 0.04$	15
0.5	$1.29 \pm 0.19$	$0.48 \pm 0.03$	$0.45 \pm 0.03$	4
1.0	$1.44 \pm 0.41$	$0.44 \pm 0.02$	$0.42 \pm 0.03$	5
3.0	$1.22 \pm 0.19$	$0.45 \pm 0.04$	$0.40 \pm 0.04$	9
7.0	$1.33 \pm 0.20$	$0.47 \pm 0.02$	$0.44 \pm 0.02$	5

blocking effect with increasing  $[\text{Na}^+]_i$ .  $I_n$ , obtained in  $50$  mM and  $110$  mM  $\text{Na}^+_o$  are compared in Table 3. Decreasing extracellular  $\text{Na}^+_o$  concentration appears to slightly enhance the  $\text{Mg}^{2+}_i$  blocking effect. These observations suggest a competitive blocking mechanism of  $\text{Mg}^{2+}$  on the sodium channel. Hence, one can propose that  $\text{Na}^+$  and  $\text{Mg}^{2+}$  competitively enter the sodium channel. The occupancy of the sodium channel by  $\text{Mg}^{2+}$ , therefore, interferes with the sodium flux in both directions.

#### Sodium channel gating mechanism is not significantly affected by $\text{Mg}^{2+}_i$

In order to investigate whether the reduction of sodium currents is an effect of  $\text{Mg}^{2+}_i$  on the gating mechanism of the sodium current we studied voltage-dependent gating parameters of sodium channels in the presence of different  $[\text{Mg}^{2+}]_i$ .

The first approach consisted of a comparison of voltage-dependent properties of peak currents in the presence of different  $[\text{Mg}^{2+}]_i$ . The time to peak,  $t_p$ , was estimated as an approximation of the activation time constant. The invariance of  $t_p$  measured at different applied potentials in the presence of  $[\text{Mg}^{2+}]_i \leq 7$  mM is presented in Table 4.

**Table 5.** Half activation potential ( $V_h$ ) and e-fold voltage dependence of activation ( $a$ ). Data were obtained from fitting the peak current, estimated at each potential, with the equation:  $I_p = g_{\max} (V_m - V_{Na}) / [1 - \exp((V_m - V_h)/a)]$  (Pröbstle et al. 1988). Values are mean  $\pm$  SD.  $[Na^+]_i = 15$  mM,  $[Na^+]_o = 110$  mM

$[Mg^{2+}]_i$	$V_h$ (mV)	$a$ (mV)	N
0.0	$10.8 \pm 2.1$	$9.9 \pm 0.9$	13
0.5	$10.5 \pm 2.1$	$10.1 \pm 1.3$	6
1.0	$9.2 \pm 1.0$	$9.4 \pm 1.2$	6
3.0	$11.8 \pm 1.9$	$10.1 \pm 1.0$	5
7.0	$10.4 \pm 3.0$	$9.6 \pm 1.2$	11

Activation curves were constructed from  $I_p$  values obtained at different concentrations of  $Mg^{2+}$ . The half activation potential,  $V_h$ , and the e-fold dependence of  $I_p$ ,  $a$ , were calculated according to Pröbstle and co-workers (1988). No significant changes of  $V_h$  and  $a$  were found when  $[Mg^{2+}]_i \leq 7$  mM, as shown in Table 5.

A further and more precise analysis of the gating mechanism of sodium channels in the presence of  $Mg^{2+}$  was performed, using the Hodgkin-Huxley model (Hodgkin and Huxley 1952), as described by Moran and Conti (1990) and Lin and Moran (1990). In this case, sodium currents measured in the presence of different  $[Mg^{2+}]_i$  were analysed.

With the addition of an empirical delay,  $\delta t$ , at the onset of the classical  $m^3h$  kinetics (Keynes and Royas 1974), sodium currents can be described as:

$$I(t) = I' \left( 1 - \exp \left( -\frac{t - \delta t}{\tau_m} \right) \right)^3 \exp \left( -\frac{t - \delta t}{\tau_h} \right), \quad (1)$$

where,  $I' = g_{\max} (V_m - V_{ref}) m_{\infty}^3 h_0$ . Fitting current traces obtained at each potential with Eq. (1) give directly the voltage dependence of activation and inactivation kinetics time constants,  $\tau_m$  and  $\tau_h$ , and that of the steady state activation parameter,  $m_{\infty}$ . We have estimated  $\tau_m$  and  $\tau_h$  at different  $[Mg^{2+}]_i$ . It was found that both  $\tau_h$  and  $\tau_m$  are not significantly different at  $[Mg^{2+}]_i \leq 7$  mM. However, the voltage-dependence of  $\tau_m$  and  $\tau_h$  do significantly shift about  $-25$  mV when  $[Mg^{2+}]_i$  is changed from 0 to 30 mM, as shown in Fig. 3A and B.

The voltage dependence of the steady-state activation parameter,  $m_{\infty}$ , is characterized by the half-activation potential,  $V_{1/2}$ , at which the open-state probability for each activation gate is 0.5, and by the apparent valence  $z_m$  of a single activation process ( $m$ -gate). These parameters were obtained by a least-squares fit to the equation

$$m_{\infty}(V_m) = \frac{1}{1 + \exp \left( z_m e_0 \frac{V_{1/2} - V_m}{k_b T} \right)}, \quad (2)$$

where,  $e_0$  is the proton charge ( $1.6 \times 10^{-19}$  Coulomb),  $k_b$  is the Boltzmann constant and  $T$  is the absolute temperature.

The voltage dependence of the steady state inactivation parameter,  $h_{\infty}$ , was obtained by fitting the peak current, obtained from traditional double-pulse experiments,

against the prepulse potential:

$$h_{\infty} \simeq \frac{I_p}{I_p^{\max}} = \frac{1}{1 + \exp \left( \frac{V_{pp} - V_{1/2}^m}{a_h} \right)}, \quad (3)$$

where,  $V_{1/2}^m$  and  $a_h$  characterize the half-inactivation potential and the steepness of the voltage-dependence.  $I_p^{\max}$  is the maximum peak current measured and  $V_{pp}$  is the prepulse potential.

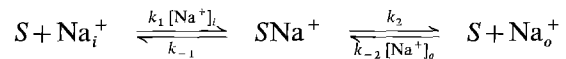
Activation and inactivation parameters, estimated with different  $[Mg^{2+}]_i$ , are compared in Table 6. Values of  $V_{1/2}^m$  and  $V_{1/2}^h$  indicate no significant difference at  $[Mg^{2+}]_i \leq 7$  mM. However, both  $V_{1/2}^m$  and  $V_{1/2}^h$  show significant negative shifts, which are in the range  $-25$  to  $-29$  mV, when  $[Mg^{2+}]_i$  was increased from 0 to 30 mM. The voltage dependence of activation and inactivation processes, expressed as  $z_m$  and  $a_h$ , do not show any significant change when  $[Mg^{2+}]_i$  is increased from 0 up to 30 mM. The voltage dependence of  $m_{\infty}$  and  $h_{\infty}$ , in the presence of 0 and 30 mM  $Mg^{2+}$ , are compared in Fig. 3C and D.

These results suggest that the effect of  $Mg^{2+}$  on sodium gating processes is non-linearly dependent on its concentration. There is a similar shift in the range  $-25$  to  $-29$  mV in the activation and inactivation processes. Nevertheless, the steepness of the voltage dependence of the gating processes, as revealed by the analysis of activation and inactivation curves, was not affected by 30 mM  $Mg^{2+}$ . This is consistent with a local surface potential change produced by  $Mg^{2+}$  on the intracellular membrane surface. Similar interpretations have been proposed by Hille (1968) and Hahn and Campbell (1983) to explain the effect of extracellular  $Ca^{2+}$  on sodium currents.

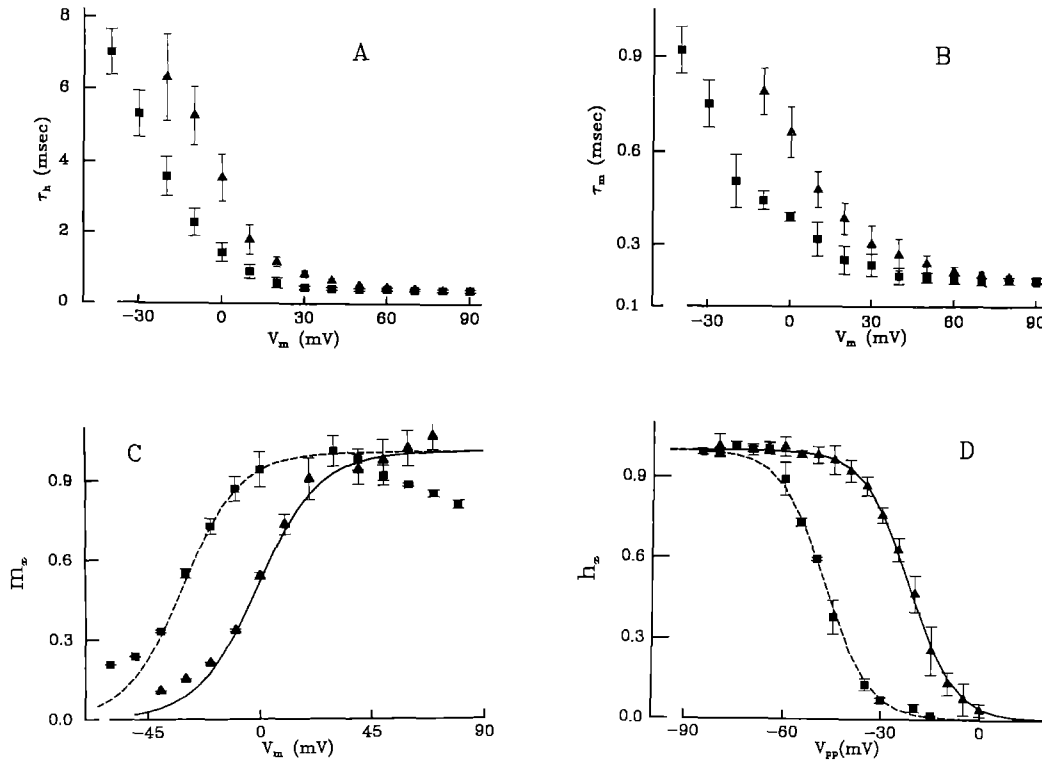
#### Kinetic model of the $Mg^{2+}$ blocking mechanism

In order to account for the dependence of the  $Mg^{2+}$  blockage on  $Na^+$  and  $Na_o^+$ , we investigated a simple permeation model based on Michaelis-Menten reaction kinetics in enzymatic reactions.

Permeation of  $Na^+$  through the sodium channel can be described as a binding process, i.e.  $Na^+$  has to bind to sites inside the channel during its passage through the membrane, and one site can bind only one ion at a time. The sodium flux depends on the rate constants of the  $Na^+$  binding and dissociation processes. The sodium permeation process can be described by the following scheme:



Although there may be more than one binding site inside the sodium channel (Hille 1975; Begenisich and Cahalan 1980a, b), we will use the one-binding site model to describe the sodium flux in order to simplify quantitative calculations, based on the assumption that the flux is mainly determined by the rate constants for  $Na^+$  with its rate-limiting site. Therefore, in the sodium permeation



**Fig. 3 A–D.** The voltage dependence of gating parameters of sodium channels. *Triangles* are values measured in the absence of  $\text{Mg}_i^{2+}$ , *squares* are those with  $[\text{Mg}_i^{2+}]_i = 30 \text{ mM}$ .  $[\text{Na}^+]_i = 30 \text{ mM}$ ,  $[\text{Na}^+]_o = 110 \text{ mM}$  in all experiments. Voltage-dependent inactivation (A) and activation (B) time constants. Each *point* represents the mean of measurements made from at least 8 different cells. *Bars* represent their standard deviations. Voltage shifts in both cases are about  $-25 \text{ mV}$ , when  $[\text{Mg}_i^{2+}]_i$  is increased from 0 to  $30 \text{ mM}$ . Time constants measured in the presence of  $7 \text{ mM}$   $\text{Mg}_i^{2+}$  (not shown) overlay quite well with those obtained at  $0 \text{ mM}$   $\text{Mg}_i^{2+}$ . C Steady state activation parameter  $m_\infty$  of sodium currents is shown as a function

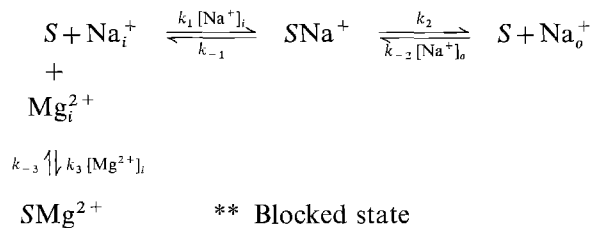
of test potential. Data points are mean values obtained from seven patches with  $0 \text{ mM}$   $\text{Mg}_i^{2+}$  and six patches with  $30 \text{ mM}$   $\text{Mg}_i^{2+}$ . *Bars* represent their standard deviations. Smooth lines were obtained by fitting data with (2).  $V_{1/2}$  shifts is  $-29.1 \pm 0.4 \text{ mV}$ . (D) Voltage dependence of steady state inactivation parameter  $h_\infty$  of sodium currents. Normalized peak inward current responses to the test pulse are plotted as a function of the prepulse potential as described in the text. Data points represent means obtained from five patches with  $0 \text{ mM}$   $\text{Mg}_i^{2+}$  and four patches with  $30 \text{ mM}$   $\text{Mg}_i^{2+}$ . Smooth lines are the least-square fitting data to (3).  $V_{1/2}$  shift is  $-25.7 \pm 7.8 \text{ mV}$

**Table 6.** Activation ( $V_{1/2}^m$ ,  $z_m$ ) and inactivation ( $V_{1/2}^h$ ,  $a_h$ ) parameters, which characterize the voltage dependence of steady state activation and inactivation parameters of the Hodgkin-Huxley model. ( $[\text{Na}^+]_i = 30 \text{ mM}$ ,  $[\text{Na}^+]_o = 110 \text{ mM}$ )

$[\text{Mg}_i^{2+}]_i$	$V_{1/2}^m$ (mV)	$z_m$	N	$V_{1/2}^h$ (mV)	$a_h$ (mV)	N
0.0	$-1.8 \pm 0.1$	$2.1 \pm 0.2$	7	$-21.8 \pm 3.9$	$-6.9 \pm 0.6$	5
0.5				$-19.2$	$-6.1$	1
1.0	$-6.5 \pm 4.3$	$2.0 \pm 0.4$	3	$-26.9$	$-6.7$	1
3.0	$-1.4$	$1.9$	1			
7.0	$-4.3 \pm 3.1$	$2.0 \pm 0.2$	5	$-26.6 \pm 4.5$	$-6.8 \pm 2.2$	2
30.0	$-30.9 \pm 0.1$	$2.2 \pm 0.2$	6	$-47.5 \pm 3.9$	$-6.9 \pm 0.3$	4

scheme above,  $S$  represents the sodium channel,  $\text{SNa}^+$  is the binding state of  $\text{Na}^+$ ,  $k$ 's represent rate constants of  $\text{Na}^+$  reactions in different directions. All of the rate constants are functions of membrane potential and depend on the chemical potential associated with their relative reactions. The binding of  $\text{Na}^+$  with its rate-limiting sites can be directly described by voltage-dependent Michaelis constants  $K_{\text{Na}_i}$  and  $K_{\text{Na}_o}$ , which are defined as:  $K_{\text{Na}_i}(V_m) = (k_{-1} + k_2)/k_1$  for  $\text{Na}_i^+$  and  $K_{\text{Na}_o}(V_m) = (k_{-1} + k_2)/k_{-2}$  for  $\text{Na}_o^+$ . In the presence of a competitive

blocker,  $\text{Mg}_i^{2+}$ , the permeation through sodium channels described above may be modified as:



where  $SMg_i^{2+}$  represents  $Mg_i^{2+}$  bound to the sodium channel  $S$ . Because no magnesium ion exists on the extracellular side of the membrane, binding of  $Mg^{2+}$  to the sodium channel can be directly characterized by a voltage-dependent dissociation constant  $K_{Mg}(V_m)$ , defined as  $K_{Mg}(V_m) = k_{-3}/k_3$ .

Therefore, the sodium flux in the presence of  $Mg_i^{2+}$  is described as:

$$I(t, V_m, [Na^+]_i, [Na^+]_o, [Mg^{2+}]_i) = \frac{\bar{I}(t, V_m, [Na^+]_i, [Na^+]_o, 0) (1 + A)}{1 + \left(1 + \frac{[Mg^{2+}]_i}{K_{Mg}(V_m)}\right) A} \quad (4)$$

where,  $A \equiv 1/(K_{Na_i}(V_m)/[Na^+]_i + K_{Na_o}(V_m)/[Na^+]_o)$ .  $I$  is the sodium current directly measured in the presence of  $Mg_i^{2+}$ . It is a function of time,  $t$ , membrane potential,  $V_m$ , and  $[Na^+]_i$ ,  $[Na^+]_o$ ,  $[Mg^{2+}]_i$ .  $\bar{I}$  is the current measured in the absence of  $Mg_i^{2+}$ . In order to supersede the time variable, the peak sodium current  $I_p$  was applied in our analysis.

$$I_p(V_m, [Na^+]_i, [Na^+]_o, [Mg^{2+}]_i) = I'_p(V_m, [Na^+]_i, [Na^+]_o, [Mg^{2+}]_i) \cdot P_0(V_m, [Na^+]_i, [Na^+]_o, [Mg^{2+}]_i), \quad (5)$$

where  $I_p$  is the peak current which can be measured directly at applied membrane potential  $V_m$ ,  $I'_p$  is the theoretical peak current when all sodium channels are in conductive states and  $P_0$  is the probability of a channel being in a conductive state. Normalizing peak current ( $I_n$ ) as:

$$I_n(V_m, [Na^+]_i, [Na^+]_o, [Mg^{2+}]_i) = \frac{I_p(V_m, [Na^+]_i, [Na^+]_o, [Mg^{2+}]_i)}{I_p(V_m, [Na^+]_i, [Na^+]_o, 0)}, \quad (6)$$

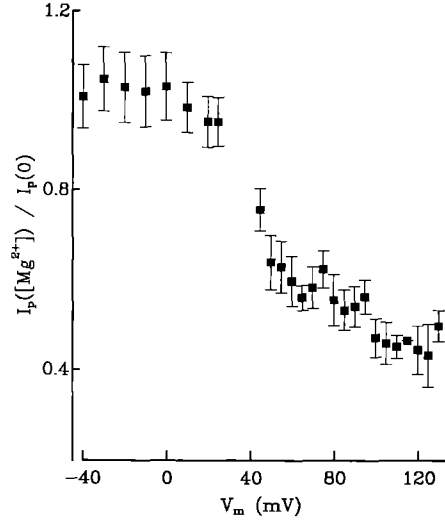
Equation (4) can be simplified to:

$$I_n(V_m, [Na^+]_i, [Na^+]_o, [Mg^{2+}]_i) = \frac{1}{1 + \frac{[Mg^{2+}]_i}{K_{Mg}^{app}(V_m, [Na^+]_i, [Na^+]_o)}}, \quad (6)$$

where the apparent binding constant  $K_{Mg}^{app}$  is defined as:

$$K_{Mg}^{app}(V_m, [Na^+]_i, [Na^+]_o) = K_{Mg}(V_m) \left(1 + \frac{[Na^+]_i}{K_{Na_i}(V_m)} + \frac{[Na^+]_o}{K_{Na_o}(V_m)}\right). \quad (7)$$

It is noteworthy that the peak current analysis method, proposed above, can be applied only if the gating mechanism of the sodium channel is not significantly influenced by  $Mg_i^{2+}$ , i.e.  $P_0$  in Eq. (5) is not significantly influenced by the presence of  $Mg_i^{2+}$ . This condition is satisfied when  $[Mg^{2+}]_i \leq 7$  mM, which has been demonstrated in the previous section (see also Tables 4, 5 and 6). If this is the case  $I_n$  would be expected to approach a constant, at least in a range where  $I'_p$  is not significantly influenced by  $Mg_i^{2+}$ . Figure 4 illustrates this behavior of  $I_n$ . It shows that  $I_n$  is quite constant at potentials lower than the sodium equilibrium potential, which is around 31 mV with 0



**Fig. 4.** Normalized sodium peak currents  $I_n$  evaluated at different membrane potentials  $V_m$ . Data points  $I_n$  were obtained by normalizing  $I_p([Mg_i^{2+}])$  obtained with 7 mM  $Mg_i^{2+}$  by  $I_p$  obtained in the absence of  $Mg_i^{2+}$ . Bars represent their standard deviations after such normalization. Normalized data points were from 23 control patches and 8  $Mg_i^{2+}$  patches. Sodium equilibrium potentials are  $30.8 \pm 2.7$  mV (0 mM  $Mg_i^{2+}$ ) and  $31.3 \pm 3.7$  mV (7 mM  $Mg_i^{2+}$ ).  $[Na^+]_i = 30$  mM and  $[Na^+]_o = 110$  mM.  $I_n$  fluctuates around 1 when membrane potential is lower than the sodium equilibrium potential, which suggests there is no significant influence of  $Mg_i^{2+}$  on the gating mechanism of the sodium channel. The decrease of  $I_n$  at membrane potentials higher than the sodium equilibrium potential indicates the voltage-dependent blockage of sodium currents by  $Mg_i^{2+}$ .

or 7 mM  $Mg_i^{2+}$ , and decreases in a voltage-dependent way when the potential increases.

$K_{Mg}^{app}$  has been calculated from  $I_n$  at different membrane potentials  $V_m$  and different ionic concentrations,  $[Na^+]_i$  and  $[Na^+]_o$ , according to Eq. (6). Its dependence on  $V_m$ ,  $[Na^+]_i$  and  $[Na^+]_o$  is illustrated in Fig. 5. The dissociation constant  $K_{Mg}(V_m)$ , Michaelis constants  $K_{Na_i}(V_m)$  and  $K_{Na_o}(V_m)$  are further obtained by fitting  $K_{Mg}^{app}$  against  $[Na^+]_i$  and  $[Na^+]_o$ , using Eq. (7). Results are represented as data points in Fig. 6.

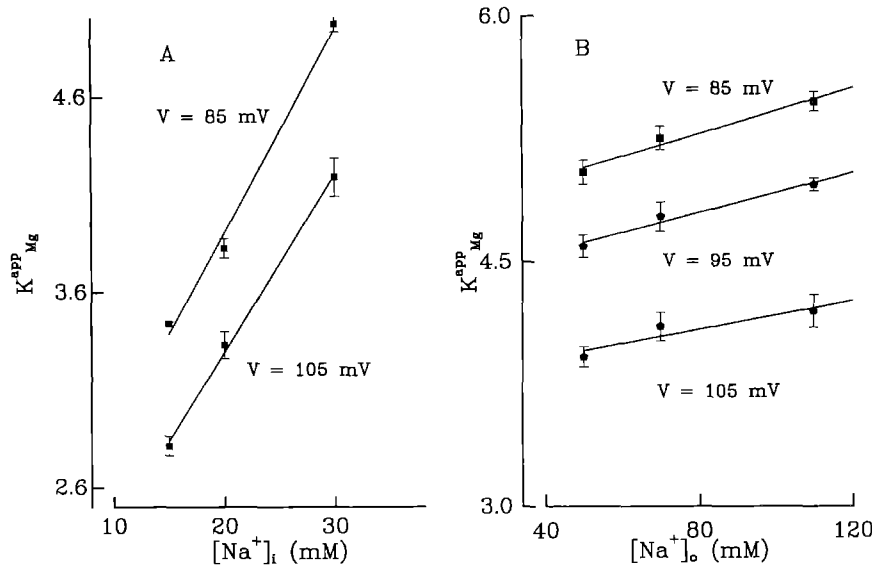
In the Appendix we show that the voltage-dependent dissociation constant  $K_{Mg}(V_m)$  of  $Mg_i^{2+}$  for the sodium channel, as well as Michaelis constants for  $Na^+$ :  $K_{Na_i}(V_m)$  and  $K_{Na_o}(V_m)$ , can be further expressed in term of the free energy of the ionic binding-dissociation process. They are given as:

$$K_{Mg}(V_m) = K_{Mg}(0) \exp(-2BV_m\delta') \quad (8)$$

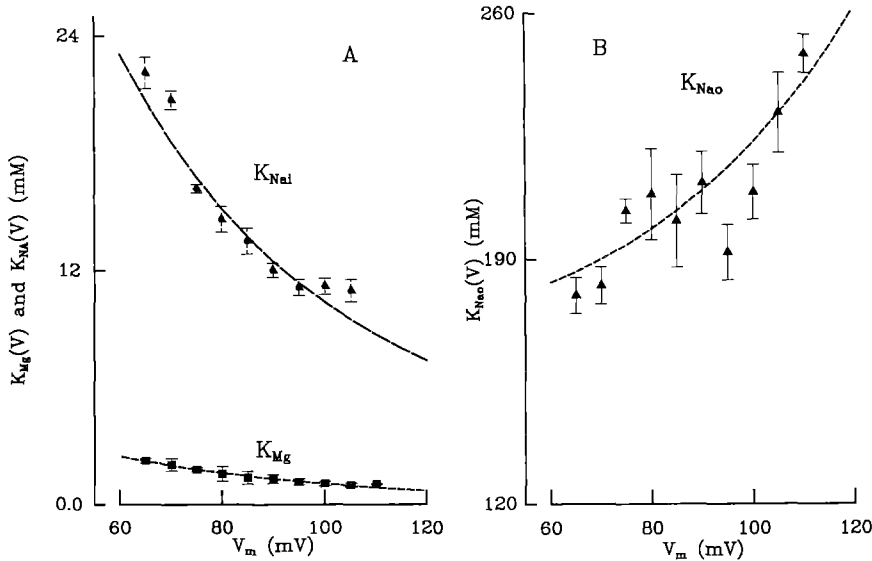
$$K_{Na_i}(V_m) = K_i(0) \exp(-BV_m\delta) + K'_i \exp\left(\frac{BV_m}{2}\right) \exp(-BV_m\delta) \quad (9)$$

$$K_{Na_o}(V_m) = K_o(0) \exp(BV_m(1-\delta)) + K'_o \exp\left(-\frac{BV_m}{2}\right) \exp(BV_m(1-\delta)), \quad (10)$$

where,  $B$  is defined as  $F/RT$ .  $F$  is the Faraday constant and  $R$  the ideal gas constant.  $\delta'$  and  $\delta$  represent the fraction of total electrical potential drop, between the inside



**Fig. 5A, B.** Apparent binding constant  $K_{Mg}^{app}$  as a function of  $[Na^+]_i$  (A) and  $[Na^+]_o$  (B).  $K_{Mg}^{app}$  were obtained from Eq. (6), at different membrane potentials  $V_m$  and different ionic concentrations  $[Na^+]_i$  and  $[Na^+]_o$ .  $K_{Mg}^{app}$  were plotted as data points in figures, bars represent their standard deviations.  $K_{Mg}^{app}$  were further fitted with Eq. (7) against  $[Na^+]_i$  with  $[Na^+]_o$  fixed at 10 mM (A), or against  $[Na^+]_o$  with  $[Na^+]_i$  fixed at 30 mM (B). Fitting results are represented as smooth lines in figures



**Fig. 6A, B.** The voltage dependence of dissociation constants  $K_{Mg}(V_m)$  (squares) and Michaelis constants  $K_{Na_i}(V_m)$  (triangles) are illustrated in A. The voltage dependence of Michaelis constant  $K_{Na_o}(V_m)$  is shown in B. Each data point was obtained by fitting  $K_{Mg}^{app}$  ( $V_m$ ,  $[Na^+]_i$ ,  $[Na^+]_o$ ) as a function of  $[Na^+]_i$  and  $[Na^+]_o$  respectively, using Eq. (7). Bars are standard deviations obtained from calculations. Smooth lines were obtained by fitting  $K_{Mg}(V_m)$  to Eq. (8) and  $K_{Na_i}(V_m)$ ,  $K_{Na_o}(V_m)$  to Eqs. (9) and (10). Fitting results are detailed in the text

surface of the membrane and the  $Mg^{2+}$  and  $Na^+$  binding sites respectively (in this text, it will be called the electrical distance from the inside).  $K_{Mg}(0)$  is the dissociation constant of  $Mg^{2+}$  for the sodium channel at zero membrane potential.  $K_{Mg}(0) = \rho^{-1} \exp(-\delta G_{Mg}/(k_B T))$ . Fixing the zero reaction free energy level at  $\rho = 1$ , which corresponds to  $K_{Mg}(0) = 1$  M, i.e. the equilibrium state, the free energy of the  $Mg^{2+}$  binding dissociation reaction,  $\delta G_{Mg}$ , can be expressed as:

$$\delta G_{Mg} = -k_B T \ln(K_{Mg}(0)) \quad (11)$$

$K_i(0) \equiv k_{-1}/k_1$  and  $K_o(0) \equiv k_2/k_{-2}$  are dissociation constants of  $Na_i^+$  and  $Na_o^+$  for the sodium channel at zero membrane potential. Relations between  $K_i(0)$  and  $K_o(0)$  and the reaction free energy are similar to Eq. (11).  $K'_i$  and  $K'_o$  represent the outward and inward sodium flux probability (see Appendix).

Values of  $K_{Mg}(V_m)$ ,  $K_{Na_i}(V_m)$  and  $K_{Na_o}(V_m)$ , obtained from Eq. (7) have been further fitted with Eqs. (8), (9) and

(10) respectively. Results are shown as smooth lines in Fig. 6. From these fittings, dissociation constants of  $Mg^{2+}$ ,  $Na_i^+$  and  $Na_o^+$  with their binding sites inside the sodium channel at  $V_m = 0$  mV have been estimated. For  $Mg^{2+}$ ,  $K_{Mg}(0)$  was estimated to be  $8.65 \pm 1.51$  mM, which corresponds to a reaction free energy of  $4.75 \pm 0.17 k_B T$ . The location of the  $Mg^{2+}$  binding site inside the sodium channel is  $0.26 \pm 0.03$  electrical distance from the inner membrane surface. The zero membrane potential dissociation constant for  $Na_i^+$ ,  $K_i(0)$ , is estimated to be  $83.76 \pm 7.60$  mM, corresponding to  $\delta G = 2.48 \pm 0.09 k_B T$ , which is smaller than that of  $Mg^{2+}$ . The location of the  $Na_i^+$  binding site is at  $0.75 \pm 0.23$  electrical distance from inner membrane surface. Finally, for extracellular  $Na^+$ , the dissociation constant  $K_o(0)$  is  $20.86 \pm 1.49$  mM with  $\delta = 0.58 \pm 0.05$  electrical distance from the inner membrane surface. The free energy of the  $Na_o^+$  binding-dissociation process is calculated to be  $3.87 \pm 0.07 k_B T$  unit, which is smaller than that for  $Na_i^+$ . This difference be-

tween  $\text{Na}_i^+$  and  $\text{Na}_o^+$  reaction free energies reflects that chemical potential differences exist between  $\text{Na}^+$  on the both sides of the membrane. This difference should lead to different favourable reaction directions for  $\text{Na}_i^+$  and  $\text{Na}_o^+$ .

## Discussion

The blockage of sodium current by intracellular  $\text{Mg}^{2+}$  already described by Pusch et al. (1989) and Pusch (1990) has been used to explain the observed reduction of outward  $\text{Na}^+$  current as a deviation from the Goldman-Hodgkin-Katz equation. The aim of this work was to investigate if this blockage also occurs in neural cells, and if it is possible to describe it in more molecular terms, based on a kinetic model.

In order to investigate if  $\text{Mg}_i^{2+}$  influences the voltage-dependent gating process of the sodium channel we analysed sodium currents in terms of the Hodgkin-Huxley model. We found no significant influence on gating parameters at  $[\text{Mg}^{2+}]_i \leq 7 \text{ mM}$ . Nevertheless, all steady-state and kinetic gating parameters show a similar shift in the range  $-25 \text{ mV}$  to  $-29 \text{ mV}$  when  $[\text{Mg}^{2+}]_i$  is increased from 0 to 30 mM, while the steepness of voltage-dependence of activation and inactivation are not affected. These equal shifts could be explained as a change of intracellular surface potential caused by  $\text{Mg}_i^{2+}$ , which screens negative charges on the inner surface and changes the local electrical field. From these findings, we concluded that the modification of the gating mechanism may enforce the reduction of sodium currents, but it is insufficient to explain  $\text{Mg}^{2+}$  blocking behaviour which is voltage-,  $[\text{Mg}^{2+}]_i$ -,  $[\text{Na}^+]_i$ - and  $[\text{Na}^+]_o$ -dependent.

We have proposed a model in which  $\text{Na}^+$  and  $\text{Mg}^{2+}$  competitively occupy the sodium channel. In this model,  $\text{Na}^+$  and  $\text{Mg}^{2+}$  have to bind to the sodium channel during their passage through the membrane. The blockage of sodium currents may be caused by  $\text{Mg}^{2+}$  occupying the sodium channel, which prevents the further binding of  $\text{Na}^+$  (if the binding site for  $\text{Mg}^{2+}$  is one of binding sites for  $\text{Na}^+$  during its passage) or interferes with the normal accommodation of  $\text{Na}^+$  by sodium channels. The sodium permeation in the presence of the competitive blocker  $\text{Mg}_i^{2+}$  has, therefore, been described as a voltage-dependent binding-unbinding process, based on Michaelis-Menten reaction kinetics. The normalized peak sodium current,  $I_n$ , has been introduced to describe quantitatively the  $\text{Mg}_i^{2+}$  blockage model, with the condition that there is no significant influence of  $\text{Mg}^{2+}$  on the gating mechanism of sodium currents. Using this simple model we can explain the  $\text{Mg}^{2+}$  blockage quite well. Furthermore, the model also provides a simple way to calculate the voltage dependence of the dissociation constant of  $\text{Mg}^{2+}$  with site  $S$ , as well as Michaelis constants for intracellular and extracellular  $\text{Na}^+$  with this site (Fig. 6). The former directly illustrates the blocking capability of  $\text{Mg}^{2+}$ . The latter two constants illustrate the influence of  $\text{Na}^+$  from different sides on the binding site as functions of membrane potential, as well as the interdependence between  $\text{Na}_i^+$  and  $\text{Na}_o^+$  in the sodium permeation.

Relations between the dissociation constant  $K_{\text{Mg}}(V_m)$ , Michaelis constants  $K_{\text{Na}_i}(V_m)$ ,  $K_{\text{Na}_o}(V_m)$  and membrane potential  $V_m$  have been further described in terms of the reaction free energy, with additive Eyring rate factors to account for the effect of the applied electrical field (see Appendix). With these relations, it provides a way to locate the binding site of  $\text{Na}^+$  and  $\text{Mg}^{2+}$  in the sodium channel. It was found that the rate-limiting binding site of  $\text{Na}_o^+$  and  $\text{Na}_i^+$  appears to be the same, it is located in the range of  $0.58 \pm 0.05$  to  $0.75 \pm 0.23$  electrical distance from the inner membrane surface. This location of the  $\text{Na}^+$  binding site,  $\delta$ , is in agreement with those calculated by others:  $1 - \delta = 0.36$  for guinea pig heart sodium channel (Nilius 1988),  $1 - \delta = 0.37 \pm 0.2$  for neuroblastoma (Yamamoto et al. 1984). Nevertheless, the rate-limiting binding site of  $\text{Mg}^{2+}$  with the sodium channel appears to be different from that of  $\text{Na}^+$ , since  $\delta' = 0.26 \pm 0.03$ . This difference supports the argument that there may be more than one binding site inside the membrane (Hille 1975; Begenisich and Cahalan 1980a, b). However, independent of how many binding sites are necessary to accurately describe the sodium current, which would lead to different transient states of  $\text{Na}^+$ , i.e.  $\text{NaS}_1$ ,  $\text{NaS}_2$  etc., in the sodium permeation scheme, the kinetic model of  $\text{Mg}_i^{2+}$  blockage we proposed is still efficient, since one binding site can bind only one ion at a time.  $\text{Mg}^{2+}$  is probably not permeable but prevents  $\text{Na}^+$  permeation by competitive binding to a site located at an electrical distance of  $0.26 \pm 0.03$  from the internal surface of the membrane.

With voltage dependent relations of dissociation constants  $K_{\text{Mg}}(V_m)$  and Michaelis constants  $K_{\text{Na}_i}(V_m)$  and  $K_{\text{Na}_o}(V_m)$ , dissociation constants of  $\text{Mg}^{2+}$  and  $\text{Na}^+$  for the sodium channel at zero membrane potential,  $K_{\text{Mg}_o}(0)$ ,  $K_i(0)$  and  $K_o(0)$  have been calculated. The value of  $K_{\text{Mg}_o}(0)$  is much smaller than that of  $K_i(0)$ , which reflects the high affinity of  $\text{Mg}^{2+}$  for the sodium channel. In fact, the reaction free energies of both reactions calculated reflect the fact that the dissociation of  $\text{Mg}^{2+}$  from the sodium channel is less energy-favorable than that of  $\text{Na}_i^+$ , since  $\delta G_{\text{Mg}} = 4.75 \pm 0.17$  and  $\delta G_i = 2.48 \pm 0.09 k_B T$ . Dissociation constants of  $\text{Na}_i^+$  and  $\text{Na}_o^+$  also appear to be different, which reflect the reaction free energy differences of  $\text{Na}_i^+$  and  $\text{Na}_o^+$ , which leads to the different effect on sodium permeation by  $\text{Na}_i^+$  and  $\text{Na}_o^+$ .

The blocking of the sodium channel by  $\text{Mg}^{2+}$  may be due to two different reasons. The first possibility is related to the selectivity of sodium channels.  $\text{Mg}^{2+}$  enters the sodium channel and binds to an inside site during membrane depolarization. Because of the selectivity of the pore (the permeability ratio of  $\text{Mg}^{2+}$  to  $\text{Na}^+$  through the sodium channel is less than 0.1 (Hille 1972)),  $\text{Mg}^{2+}$  is not further permeable and is even kicked back due to the small extracellular  $\text{Na}^+$  inward flux through the channel. The other possibility is that the strong binding force between  $\text{Mg}^{2+}$  and the site retards the release of  $\text{Mg}^{2+}$  from the channel. In fact, the dissociation constant value for  $\text{Mg}^{2+}$  binding within the sodium channel at zero membrane potential, is  $8.65 \pm 1.51 \text{ mM}$ , which is much smaller than that for  $\text{Na}_i^+$ :  $K_i(0) = 83.76 \pm 7.60 \text{ mM}$ . Most probably, these two possibilities may coexist and influence each other, which may lead to the entrance of  $\text{Mg}^{2+}$  into the



channel several times during the depolarization, giving a high frequency of flickering at the single channel level and thus produce an apparent single channel conductance decrease. This phenomenon has been observed in single channel measurements of a mutant sodium channel expressed in *Xenopus* oocytes (Pusch 1990). However, before choosing between these hypotheses, more experiments on the microscopic properties of the wild-type sodium channel, either in cells or expressed in oocytes, are needed.

The data presented here have shown that sodium currents of rat cerebellar granule cells can be blocked by intracellular magnesium in a voltage- and concentration-dependent manner, by  $\text{Na}^+$  and  $\text{Mg}^{2+}$  competitively occupying the sodium channel. In a summary, we could get some general information from our analysis: (1) The affinity of  $\text{Mg}^{2+}$  for sodium channels is much higher than those of  $\text{Na}_i^+$  and  $\text{Na}_o^+$ . At zero membrane potential, ionic affinities with sodium channels satisfy the relation  $\text{Na}_i^+ < \text{Na}_o^+ < \text{Mg}^{2+}$ . (2) The entrance of  $\text{Mg}^{2+}$  into the channel may be blocked at a site very close to the intracellular membrane surface. This location differs from that of the  $\text{Na}^+$  rate-limiting binding site.

From our results, the half blocking concentration of  $\text{Mg}_i^{2+}$  is shown to be a decreasing function of applied membrane potential:  $K_{\text{Mg}}$  is  $8.65 \pm 1.51 \text{ mM}$  at  $0 \text{ mV}$ ;  $1.37 \pm 0.33 \text{ mM}$  at  $85 \text{ mV}$  and  $0.99 \pm 0.10 \text{ mM}$  at  $105 \text{ mV}$ . Dissociation constants obtained at high membrane potentials are comparable with the physiological intracellular  $\text{Mg}^{2+}$  concentration, which should be in the order of  $1.7 \text{ mM}$ , as measured in frog skeletal muscle (Alvarez-Leefmans et al. 1986). Our data suggest that the physiological  $\text{Mg}_i^{2+}$  concentration is sufficient to block sodium channels significantly when cells are exposed to considerable depolarization. This effect may correspond to a physiological regulation mechanism of sodium channels.

## Appendix

### The free energy of the reaction

A general process for the ionic binding-dissociation reaction, as indicated in our kinetic scheme for sodium permeation, can be described in terms of tunneling through barriers and wells. The corresponding partition function is the sum over all possible configurations of the reaction with appropriate Boltzmann factors. In terms of path-integral formalism, the partition function is given by

$$\Xi = \frac{1}{N} \int \mathcal{D} \phi \exp \left( - \frac{G[\phi]}{k_B T} \right), \quad (\text{A-1})$$

where,  $\phi$  is a general configuration of the reaction,  $G[\phi]$  is the free energy function,  $k_B$  is the Boltzmann constant,  $T$  is the absolute temperature and  $N$  is a normalization factor.

For the  $\text{Mg}_i^{2+}$  dissociation reaction, the dissociation rate constant,  $k_{-3}$ , can be expressed as

$$k_{-3} = \int \mathcal{D} \phi 2\pi \omega[\phi] \exp \left( - \frac{G[\phi]}{k_B T} \right) \quad (\text{A-2})$$

in which,  $2\pi \omega[\phi]$  is the reaction rate for a given configuration  $\phi$ . In the case of heavy ions, e.g.  $\text{Mg}^{2+}$  and  $\text{Na}^+$ , fluctuation effects can be ignored and a saddle point approximation is valid. In this approximation, we have

$$k_{-3} = 2\pi \omega_{-3} \exp \left( - \frac{G_{\text{Mg}}^-}{k_B T} \right) \quad (\text{A-3-a})$$

where,  $G_{\text{Mg}}^-$  is the free energy associated with the most probable configuration of the dissociation reaction, and  $2\pi \omega_{-3}$  is the corresponding reaction rate which can be further expressed in terms of the thermal energy  $k_B T$ , i.e.  $2\pi \omega_{-3} = k_B T/h$ , where  $h$  is the Planck constant.

Analogously, the rate constant of the  $\text{Mg}^{2+}$  binding process can be expressed as

$$k_3 = \varrho \frac{k_B T}{h} \exp \left( - \frac{G_{\text{Mg}}^+}{k_B T} \right) \quad (\text{A-3-b})$$

where  $G_{\text{Mg}}^+$  is the free energy of the binding reaction.  $\varrho$  is a constant with the dimension of  $\text{M}^{-1}$ , to be fixed by the zero-free energy level of the reaction.

Similarly, binding and dissociation rate constants for  $\text{Na}_i^+$  and  $\text{Na}_o^+$  are expressed as

$$k_1 = \varrho_i \frac{k_B T}{h} \exp \left( - \frac{G_i^+}{k_B T} \right) \quad (\text{A-3-c})$$

$$k_{-1} = \frac{k_B T}{h} \exp \left( - \frac{G_i^-}{k_B T} \right) \quad (\text{A-3-d})$$

$$k_{-2} = \varrho_o \frac{k_B T}{h} \exp \left( - \frac{G_o^+}{k_B T} \right) \quad (\text{A-3-e})$$

$$k_2 = \frac{k_B T}{h} \exp \left( - \frac{G_o^-}{k_B T} \right) \quad (\text{A-3-f})$$

in which, subscripts of  $G$ , 'i' and 'o' refer to reactions of  $\text{Na}_i^+$  and  $\text{Na}_o^+$  respectively. '+' and '-' refer the binding and dissociation processes.  $\varrho_i$  and  $\varrho_o$  are constants fixed by zero-free energy levels for reactions of  $\text{Na}_i^+$  and  $\text{Na}_o^+$ .

In the presence of an applied membrane potential  $V_m$ , additional Eyring rate factors (Eyring 1935) have to be included in equations (A-3), in order to take into account the electrical field effect introduced. Therefore, the dissociation constant of  $\text{Mg}^{2+}$  is:

$$K_{\text{Mg}}(V_m) \equiv \frac{k_{-3}}{k_3} = K_{\text{Mg}}(0) \exp(-2BV_m \delta'). \quad (\text{A-4})$$

Analogously, voltage-dependent Michaelis constants,  $K_{\text{Na}_i}(V_m)$  and  $K_{\text{Na}_o}(V_m)$ , are expressed as:

$$K_{\text{Na}_i}(V_m) \equiv \frac{k_{-1} + k_1}{k_1} = K_i(0) \exp(-BV_m \delta) + K'_i \exp \left( \frac{BV_m}{2} \right) \exp(-BV_m \delta) \quad (\text{A-4})$$

$$K_{\text{Na}_o}(V_m) \equiv \frac{k_{-1} + k_1}{k_1} = K_o(0) \exp(BV_m(1-\delta)) + K'_o \exp \left( - \frac{BV_m}{2} \right) \exp(BV_m(1-\delta)) \quad (\text{A-5})$$

in which,  $B$  is defined as  $F/RT$ .  $\delta'$  and  $\delta$  represent the fraction of total electrical potential drop, between the inside surface of the membrane and the  $\text{Mg}^{2+}$  and  $\text{Na}^+$

binding sites respectively (the total electrical potential drop across the membrane is assumed to be 1).

$$K_i' \equiv \frac{1}{q_i} \exp \left( -\frac{G_o^- - G_i^+}{k_B T} \right)$$

and

$$K_o' \equiv \frac{1}{q_o} \exp \left( -\frac{G_i^- - G_o^+}{k_B T} \right).$$

$K_{Mg}(0)$ ,  $K_i(0)$  and  $K_o(0)$  are the dissociation constants of  $Mg^{2+}$ ,  $Na_i^+$  and  $Na_o^+$  for the sodium channel at zero membrane potential. They are defined as

$$K_{Mg}(0) = \frac{1}{q} \exp \left( -\frac{\delta G_{Mg}}{k_B T} \right),$$

$$K_i(0) = \frac{1}{q_i} \exp \left( -\frac{\delta G_i}{k_B T} \right)$$

and

$$K_o(0) = \frac{1}{q_o} \exp \left( -\frac{\delta G_o}{k_B T} \right)$$

where  $\delta G$  represents different ionic binding-dissociation reaction free energies at zero membrane potential, with subscripts related to  $Mg^{2+}$ ,  $Na_i^+$  and  $Na_o^+$ .

Fixing the zero-free energy level at  $q=1$ , which corresponds to dissociation constants of 1 M, i.e. fixing the zero-free energy levels at equilibrium states at  $V=0$  mV, free energies of reactions of  $Mg^{2+}$ ,  $Na_i^+$  and  $Na_o^+$  systems can be calculated as:

$$\delta G_{Mg} = -k_B T \ln K_{Mg}(0) \quad (A-7)$$

$$\delta G_i = -k_B T \ln K_i(0) \quad (A-8)$$

$$\delta G_o = -k_B T \ln K_o(0) \quad (A-9)$$

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